5-10 Dividing Mixed Numbers - Practice and Problem Solving

Divide. Write in simplest form.

7.
$$4\frac{1}{6} \div 10$$

$$4\frac{1}{6} \div 10 = \frac{25}{6} \div \frac{10}{1}$$
$$= \frac{25}{6} \times \frac{1}{10}$$
$$= \frac{25}{6} \times \frac{1}{10}$$
$$= \frac{25 \times 1}{6 \times 10}$$
$$= \frac{5}{12}$$

9.
$$6 \div 2\frac{1}{4}$$

$$6 \div 2\frac{1}{4} = \frac{6}{1} \div \frac{9}{4}$$

$$= \frac{6}{1} \times \frac{4}{9}$$

$$= \frac{\cancel{6} \times 4}{\cancel{1} \times \cancel{9}}$$

$$= \frac{\cancel{8} \text{ or } 2\frac{2}{3}$$

11.
$$7\frac{4}{5} \div \frac{1}{5}$$

$$7\frac{4}{5} \div \frac{1}{5} = \frac{39}{5} \div \frac{1}{5}$$
$$= \frac{39}{5} \times \frac{5}{1}$$
$$= \frac{39 \times \cancel{5}}{\cancel{5} \times 1}$$
$$= \frac{39}{1} \text{ or } 39$$

13.
$$8\frac{3}{4} \div 2\frac{1}{6}$$

$$8\frac{3}{4} \div 2\frac{1}{6} = \frac{35}{4} \div \frac{13}{6}$$

$$= \frac{35}{4} \times \frac{6}{13}$$

$$= \frac{35 \times \cancel{6}}{\cancel{4} \times 13}$$

$$= \frac{105}{26} \text{ or } 4\frac{1}{26}$$

15.
$$3\frac{3}{4} \div 5\frac{5}{8}$$

$$3\frac{3}{4} \div 5\frac{5}{8} = \frac{15}{4} \div \frac{45}{8}$$
$$= \frac{15}{4} \times \frac{8}{45}$$
$$= \frac{\cancel{15} \times \cancel{8}}{\cancel{15} \times \cancel{15}}$$
$$= \frac{2}{\cancel{3}}$$

17.
$$6\frac{3}{5} \div 2\frac{3}{4}$$

$$6\frac{3}{5} \div 2\frac{3}{4} = \frac{33}{5} \div \frac{11}{4}$$

$$= \frac{33}{5} \times \frac{4}{11}$$

$$= \frac{\cancel{33} \times 4}{\cancel{5} \times \cancel{11}}$$

$$= \frac{12}{5} \text{ or } 2\frac{2}{5}$$

ALGEBRA Evaluate each expression if $a = 4\frac{4}{5}$, $b = \frac{2}{3}$, c = 6, and $d = 1\frac{1}{2}$.

19.
$$b \div 1\frac{2}{9}$$

$$b \div 1\frac{2}{9} = \frac{2}{3} \div \frac{11}{9}$$
$$= \frac{2}{3} \times \frac{9}{11}$$
$$= \frac{2 \times \cancel{9}}{\cancel{5} \times 11}$$
$$= \frac{6}{11}$$

21. $a \div c$

$$a \div c = 4\frac{4}{5} \div 6$$

$$= \frac{24}{5} \div \frac{6}{1}$$

$$= \frac{24}{5} \times \frac{1}{6}$$

$$= \frac{\cancel{24} \times 1}{\cancel{5} \times \cancel{6}}$$

$$= \frac{4}{5}$$

23.
$$c \div (ab)$$

$$c \div (ab) = 6 \div \left(4\frac{4}{5} \times \frac{2}{3}\right)$$

$$= 6 \div \left(\frac{24}{5} \times \frac{2}{3}\right)$$

$$= 6 \div \left(\frac{\cancel{24} \times 2}{5 \times \cancel{3}}\right)$$

$$= 6 \div \frac{16}{5}$$

$$= \frac{6}{1} \times \frac{5}{16}$$

$$= \frac{\cancel{6} \times 5}{1 \times \cancel{16}}$$

$$= \frac{15}{8} \text{ or } 1\frac{7}{8}$$

25. MEASUREMENT Suppose you are designing the layout for your school yearbook. If a student photograph is $1\frac{3}{8}$ inches wide, how many photographs will fit across a page that is $6\frac{7}{8}$ inches wide? Assume there is no spacing between photographs.

$$13\frac{1}{2} \div 2\frac{1}{4} = \frac{27}{2} \div \frac{9}{4}$$

$$= \frac{27}{2} \times \frac{4}{9}$$

$$= \frac{\cancel{21} \times \cancel{4}}{\cancel{21} \times \cancel{4}}$$

$$= \frac{6}{1} \text{ or } 6$$

Six photographs will fit on a page.

BORDERS The length of a kitchen wall is $24\frac{2}{3}$ feet long. A border will be placed along the wall of the kitchen. If the border comes in strips that are each $1\frac{3}{4}$ feet long, how many strips of border are needed?

Divide the length of the kitchen wall by the length of the strip of border.

$$24\frac{2}{3} \div 1\frac{3}{4} = \frac{74}{3} \div \frac{7}{4}$$
$$= \frac{74}{3} \times \frac{4}{7}$$
$$= \frac{296}{21}$$
$$= 14\frac{2}{21}$$

15 strips will be needed.

HURRICANES Use the following information.

Suppose a hurricane traveled 130 miles from a point in the Atlantic Ocean to the Florida coastline in $6\frac{1}{2}$ hours.

29. How many miles per hour did the hurricane travel?

Speed = distance
$$\div$$
 time

$$= 130 \div 6\frac{1}{2}$$

$$= 130 \div \frac{13}{2}$$

$$= 130 \times \frac{2}{13}$$

$$= \frac{130 \times 2}{13}$$

$$= \frac{260}{13}$$

The hurricane traveled at a speed of 20 mph.

OPEN ENDED Find two mixed numbers with a quotient of $2\frac{2}{3}$

Sample answer: $8\frac{2}{3} \div 3\frac{1}{4}$

CHALLENGE Without dividing, explain whether $5\frac{1}{6} \div 3\frac{5}{8}$ is greater than or less than $5\frac{1}{6} \div 2\frac{2}{5}$.

less than; Sample answer: since $3\frac{5}{8} > 2\frac{2}{5}$, the quotient $5\frac{1}{6} \div 3\frac{5}{8} < 5\frac{1}{6} \div 2\frac{2}{5}$. The expression $5\frac{1}{6} \div 3\frac{5}{8}$ represents $5\frac{1}{6}$ being divided into a greater number of parts than the expression $5\frac{1}{6} \div 2\frac{2}{5}$. If $5\frac{1}{6}$ is divided into a greater number of parts, each part will be smaller.

- The largest meteorite crater is in Winslow, Arizona, with a depth of about $\frac{2}{50}$ mile and a distance across of about $\frac{4}{5}$ mile. How many times greater is the distance across the meteorite than its depth?
 - A about 20
 - **B** about $15\frac{1}{2}$
 - C about $5\frac{1}{2}$
 - **D** about 5

$$\frac{4}{5} \div \frac{2}{50} = \frac{4}{5} \times \frac{50}{2}$$
$$= \frac{2}{1} \times \frac{10}{1}$$
$$= \frac{20 \times 1}{1 \times 1}$$
$$= \frac{20}{1} \text{ or } 20$$

It is about 20 times greater in distance across the meteorite than in depth.

37. If a quart is $\frac{1}{4}$ of a gallon and a pint is $\frac{1}{8}$ of a gallon, how much of a quart is a pint?

$$\frac{1}{8} \div \frac{1}{4} = \frac{1}{8} \times \frac{4}{1}$$
$$= \frac{1}{4} \times \frac{2}{1}$$
$$= \frac{2}{4} = \frac{1}{2}$$

$$\frac{1}{2}$$
 qt

Multiply. Write in simplest form.

39.
$$\frac{4}{5} \times 1\frac{3}{4}$$

$$\frac{4}{5} \times 1\frac{3}{4} = \frac{4}{5} \times \frac{7}{4}$$
$$= \frac{\cancel{\cancel{4}} \times 7}{5 \times \cancel{\cancel{4}}}$$
$$= \frac{7}{5} \text{ or } 1\frac{2}{5}$$

41.
$$1\frac{1}{8} \times 5\frac{1}{3}$$

$$1\frac{1}{8} \times 5\frac{1}{3} = \frac{9}{8} \times \frac{16}{3}$$
$$= \frac{\cancel{9} \times \cancel{16}}{\cancel{8} \times \cancel{3}}$$
$$= \frac{6}{1} \text{ or } 6$$