

5-9 Dividing Fractions - Practice and Problem Solving

Find the reciprocal of each number.

13. $\frac{1}{10}$

Since $\frac{1}{10} \times \frac{10}{1} = 1$, the reciprocal of $\frac{1}{10}$ is $\frac{10}{1}$ or 10.

15. $\frac{7}{9}$

Since $\frac{7}{9} \times \frac{9}{7} = 1$, the reciprocal of $\frac{7}{9}$ is $\frac{9}{7}$.

17. 1

Since $1 \times 1 = 1$, the reciprocal of 1 is 1.

Divide. Write in simplest form.

19. $\frac{1}{2} \div \frac{2}{3}$

$$\begin{aligned}\frac{1}{2} \div \frac{2}{3} &= \frac{1}{2} \times \frac{3}{2} \\ &= \frac{1 \times 3}{2 \times 2} \\ &= \frac{3}{4}\end{aligned}$$

21. $\frac{3}{4} \div \frac{9}{10}$

$$\begin{aligned}\frac{3}{4} \div \frac{9}{10} &= \frac{3}{4} \times \frac{10}{9} \\ &= \frac{\overset{1}{\cancel{3}} \times \overset{5}{\cancel{10}}}{\underset{2}{\cancel{4}} \times \underset{3}{\cancel{9}}} \\ &= \frac{5}{6}\end{aligned}$$

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23. $2 \div \frac{3}{5}$

$$\begin{aligned} 2 \div \frac{3}{5} &= \frac{2}{1} \times \frac{5}{3} \\ &= \frac{2 \times 5}{1 \times 3} \\ &= \frac{10}{3} \text{ or } 3\frac{1}{3} \end{aligned}$$

25. $8 \div \frac{4}{7}$

$$\begin{aligned} 8 \div \frac{4}{7} &= \frac{8}{1} \times \frac{7}{4} \\ &= \frac{\overset{2}{\cancel{8}} \times 7}{1 \times \underset{1}{\cancel{4}}} \\ &= 14 \end{aligned}$$

27. $\frac{5}{6} \div 5$

$$\begin{aligned} \frac{5}{6} \div 5 &= \frac{5}{6} \times \frac{1}{5} \\ &= \frac{\overset{1}{\cancel{5}} \times 1}{6 \times \underset{1}{\cancel{5}}} \\ &= \frac{1}{6} \end{aligned}$$

29. $\frac{8}{9} \div 4$

$$\begin{aligned} \frac{8}{9} \div 4 &= \frac{8}{9} \times \frac{1}{4} \\ &= \frac{\overset{2}{\cancel{8}} \times 1}{9 \times \underset{1}{\cancel{4}}} \\ &= \frac{2}{9} \end{aligned}$$

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31. **MEASUREMENT** Jamar has a piece of plywood that is $\frac{8}{9}$ yard long. He wants to cut this into 3 equal-size pieces to use as small shelves in his bedroom. What will be the length of each of these shelves?

$$\begin{aligned}\frac{8}{9} \div 3 &= \frac{8}{9} \times \frac{1}{3} \\ &= \frac{8 \times 1}{9 \times 3} \\ &= \frac{8}{27}\end{aligned}$$

Each shelf will be $\frac{8}{27}$ yd long.

33. **MEASUREMENT** A piece of string is to be cut into equal-size pieces. If the length of the string is $\frac{11}{12}$ foot long and each piece is to be $\frac{1}{24}$ foot long, how many pieces can be cut?

$$\begin{aligned}\frac{11}{12} \div \frac{1}{24} &= \frac{11}{12} \times \frac{24}{1} \\ &= \frac{11 \times \overset{2}{\cancel{24}}}{\underset{1}{\cancel{12}} \times 1} \\ &= 22\end{aligned}$$

22 pieces can be cut.

CRAFTS Refer to the following information.

To tie-dye one T-shirt, $\frac{3}{8}$ of a cup of dye is needed. The table shows the number of cups of each color of dye in Mr. Nielson's art class.

Amount of Dye	
Color	Number of Cups
red	12
orange	$3\frac{3}{4}$
yellow	2
green	$2\frac{5}{6}$
blue	8
purple	$5\frac{1}{2}$
black	6

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35. Mr. Nielson has three classes. For each class, he wants to use the same amount of red dye. How many T-shirts can be made using only the color red for each class?

$$12 \div 3 = 4;$$

$$4 \div \frac{3}{8} = \frac{4}{1} \div \frac{3}{8} = \frac{4}{1} \times \frac{8}{3} \\ = \frac{32}{3} \text{ or } 10\frac{2}{3}$$

10 shirts can be made using only red dye.

ALGEBRA Use the order of operations to evaluate each expression if $a = \frac{2}{3}$, $b = \frac{3}{4}$, and $c = \frac{1}{2}$.

37. $b \div c - a$

$$b \div c - a = \frac{3}{4} \div \frac{1}{2} - \frac{2}{3} \\ = \frac{3}{4} \times \frac{2}{1} - \frac{2}{3} \\ = \frac{3 \times \overset{1}{\cancel{2}}}{\underset{2}{\cancel{4}} \times 1} - \frac{2}{3} \\ = \frac{3}{2} - \frac{2}{3} \\ = \frac{3 \times 3}{2 \times 3} - \frac{2 \times 2}{3 \times 2} \\ = \frac{9}{6} - \frac{4}{6} \\ = \frac{5}{6}$$

39. $c \div b + a$

$$c \div b + a = \frac{1}{2} \div \frac{3}{4} + \frac{2}{3} \\ = \frac{1}{2} \times \frac{4}{3} + \frac{2}{3} \\ = \frac{1 \times \overset{2}{\cancel{4}}}{\underset{1}{\cancel{2}} \times 3} + \frac{2}{3} \\ = \frac{2}{3} + \frac{2}{3} \\ = \frac{4}{3} \text{ or } 1\frac{1}{3}$$

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41. **FIND THE DATA** Refer to the Data File on pages 16-19. Choose some data and write a real-world problem in which you would divide fractions.

See students' work.

43. **FIND THE ERROR** Raul and Tom are solving $\frac{8}{9} \div 4$. Who is correct? Explain your reasoning.

Raul		Tom
$\frac{8}{9} \div 4 = \frac{8}{9} \times \frac{4}{1}$ $= \frac{32}{9}$ or $3\frac{5}{9}$		$\frac{8}{9} \div 4 = \frac{8}{9} \times \frac{1}{4}$ $= \frac{8}{36}$ or $\frac{2}{9}$

Tom; To divide by 4, multiply by the reciprocal, which is $\frac{1}{4}$.

CHALLENGE Simplify each expression. Then, write one or two sentences describing each result

45. $\frac{a}{b} \div \frac{c}{b}$

$\frac{a}{c}$; Sample answer: if the denominators of two fractions are the same, then the quotient of the first fraction divided by the second fraction will be a fraction whose numerator is the numerator of the first fraction and whose denominator is the numerator of the second fraction.

47. In cooking, 1 drop is equal to $\frac{1}{6}$ of a dash. If a recipe calls for $\frac{2}{3}$ of a dash, which expression would give the number of drops that are needed?

A $\frac{1}{6} + \frac{2}{3}$

B $\frac{1}{6} - \frac{2}{3}$

C $\frac{1}{6} \times \frac{2}{3}$

D $\frac{2}{3} \div \frac{1}{6}$

D $\frac{2}{3} \div \frac{1}{6}$

Multiply. Write in simplest form

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49. $2\frac{2}{5} \times 3\frac{1}{3}$

$$\begin{aligned} 2\frac{2}{5} \times 3\frac{1}{3} &= \frac{12}{5} \times \frac{10}{3} \\ &= \frac{\overset{4}{\cancel{12}} \times \overset{2}{\cancel{10}}}{\underset{1}{\cancel{5}} \times \underset{1}{\cancel{3}}} \\ &= \frac{8}{1} \text{ or } 8 \end{aligned}$$

51. $3\frac{3}{7} \times 2\frac{3}{8}$

$$\begin{aligned} 3\frac{3}{7} \times 2\frac{3}{8} &= \frac{24}{7} \times \frac{19}{8} \\ &= \frac{\overset{3}{\cancel{24}} \times 19}{7 \times \underset{1}{\cancel{8}}} \\ &= \frac{57}{7} \\ &= 8\frac{1}{7} \end{aligned}$$

53. **VOLUNTEERING** According to a survey, 9 in 10 teens volunteer at least once a year. Of these, about $\frac{1}{3}$ help clean up their communities. What fraction of teens volunteer by helping clean up their communities?

$$\begin{aligned} \frac{9}{10} \times \frac{1}{3} &= \frac{\overset{3}{\cancel{9}} \times 1}{10 \times \underset{1}{\cancel{3}}} \\ &= \frac{3}{10} \end{aligned}$$

$\frac{3}{10}$ of teens help by cleaning up their communities.

PREREQUISITE SKILL Write each mixed number as an improper fraction. Then find the reciprocal of each.

55. $1\frac{2}{3}$

$$1\frac{2}{3} = \frac{(1 \times 3) + 2}{3} = \frac{5}{3}$$

Since $\frac{5}{3} \times \frac{3}{5} = 1$, the reciprocal of $\frac{5}{3}$ is $\frac{3}{5}$.

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57. $4\frac{1}{2}$

$$4\frac{1}{2} = \frac{(4 \times 2) + 1}{2} = \frac{9}{2}$$

Since $\frac{9}{2} \times \frac{2}{9} = 1$, the reciprocal of $\frac{9}{2}$ is $\frac{2}{9}$.

59. $6\frac{4}{5}$

$$6\frac{4}{5} = \frac{(6 \times 5) + 4}{5} = \frac{34}{5}$$

Since $\frac{34}{5} \times \frac{5}{34} = 1$, the reciprocal of $\frac{34}{5}$ is $\frac{5}{34}$.